

TABLA DE DERIVADAS

FUNCIÓN	FUNCIÓN DERIVADA	FUNCIÓN	FUNCIÓN DERIVADA
a	0	sen x	cos x
x	1	sen u	u' cos u
x ²	2x	cos x	- sen x
x ^m	m · x ^{m-1}	cos u	- u' sen u
f(x) + g(x)	f'(x) + g'(x)	tg x	$\frac{1}{\cos^2 x} = 1 + \operatorname{tg}^2 x$
k · f(x)	k · f'(x)	tgu	$\frac{u'}{\cos^2 u}$
f(x) · g(x)	f'(x) · g(x) + f(x) · g'(x)	cot g x	$\frac{-1}{\operatorname{sen}^2 x} = -(1 + \operatorname{cot}^2 x)$
$\frac{f(x)}{g(x)}$	$\frac{f'(x) \cdot g(x) - f(x) \cdot g'(x)}{g^2(x)}$	cot g u	$\frac{-u'}{\operatorname{sen}^2 u} = -(1 + \operatorname{cot}^2 u) \cdot u'$
$\frac{1}{f(x)}$	$\frac{-f'(x)}{f^2(x)}$	sec x	tg x · sec x
(f ∘ g)(x)	f'(g(x)) · g'(x)	sec u	u' · tg u · sec u
u ^m	m · u ^{m-1} · u'	cosec x	- cot g x · cosec x
ln x	$\frac{1}{x}$	cosec u	- u' · cot g u · cosec u
ln u	$\frac{u'}{u}$	arc sen x	$\frac{1}{\sqrt{1-x^2}}$
$\lg_a x = \frac{\ln x}{\ln a}$	$\frac{1}{x \ln a}$	arc sen u	$\frac{u'}{\sqrt{1-u^2}}$
$\lg_a u$	$\frac{u'}{u \ln a}$	arc cos x	$\frac{-1}{\sqrt{1-x^2}}$
e ^x	e ^x	arc cos u	$\frac{-u'}{\sqrt{1-u^2}}$
e ^u	u' e ^u	arc tg x	$\frac{1}{1+x^2}$
a ^x	a ^x · ln a	arc tgu	$\frac{u'}{1+u^2}$
a ^u	a ^u · ln a · u'	arc ctg x	$\frac{-1}{1+x^2}$
u ^v	$u^v \left(v' \ln u + \frac{v \cdot u'}{u} \right)$	arc ctg u	$\frac{-u'}{1+u^2}$

a, k, m son constantes

u, v, f, g, son funciones de la variable x

FÓRMULAS DE TRIGONOMETRIA

$\operatorname{sen} \alpha = \frac{\text{cat. opuesto}}{\text{hipotenusa}}$	$\operatorname{cos} \alpha = \frac{\text{cat. adyacente}}{\text{hipotenusa}}$	$\operatorname{tg} \alpha = \frac{\text{cat. opuesto}}{\text{cat. adyacente}} = \frac{\operatorname{sen} \alpha}{\operatorname{cos} \alpha}$
$\operatorname{cosec} \alpha = \frac{1}{\operatorname{sen} \alpha}$	$\operatorname{sec} \alpha = \frac{1}{\operatorname{cos} \alpha}$	$\operatorname{tg} \alpha = \frac{1}{\operatorname{cot} \alpha}$
$\operatorname{sen}^2 \alpha + \operatorname{cos}^2 \alpha = 1$	$1 + \operatorname{tg}^2 \alpha = \operatorname{sec}^2 \alpha$	$1 + \operatorname{cot}^2 \alpha = \operatorname{cosec}^2 \alpha$
$\operatorname{sen}(\alpha + \beta) = \operatorname{sen} \alpha \cdot \operatorname{cos} \beta + \operatorname{cos} \alpha \cdot \operatorname{sen} \beta$	$\operatorname{sen} 2\alpha = 2 \cdot \operatorname{sen} \alpha \cdot \operatorname{cos} \alpha$	$\operatorname{sen} \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \operatorname{cos} \alpha}{2}}$
$\operatorname{sen}(\alpha - \beta) = \operatorname{sen} \alpha \cdot \operatorname{cos} \beta - \operatorname{cos} \alpha \cdot \operatorname{sen} \beta$		
$\operatorname{cos}(\alpha + \beta) = \operatorname{cos} \alpha \cdot \operatorname{cos} \beta - \operatorname{sen} \alpha \cdot \operatorname{sen} \beta$	$\operatorname{cos} 2\alpha = \operatorname{cos}^2 \alpha - \operatorname{sen}^2 \alpha$	$\operatorname{cos} \frac{\alpha}{2} = \pm \sqrt{\frac{1 + \operatorname{cos} \alpha}{2}}$
$\operatorname{cos}(\alpha - \beta) = \operatorname{cos} \alpha \cdot \operatorname{cos} \beta + \operatorname{sen} \alpha \cdot \operatorname{sen} \beta$		
$\operatorname{tg}(\alpha + \beta) = \frac{\operatorname{tg} \alpha + \operatorname{tg} \beta}{1 - \operatorname{tg} \alpha \cdot \operatorname{tg} \beta}$	$\operatorname{tg} 2\alpha = \frac{2 \operatorname{tg} \alpha}{1 - \operatorname{tg}^2 \alpha}$	$\operatorname{tg} \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \operatorname{cos} \alpha}{1 + \operatorname{cos} \alpha}}$
$\operatorname{sen} A + \operatorname{sen} B = 2 \cdot \operatorname{sen} \frac{A+B}{2} \cdot \operatorname{cos} \frac{A-B}{2}$	$\operatorname{cos} A + \operatorname{cos} B = 2 \cdot \operatorname{cos} \frac{A+B}{2} \cdot \operatorname{cos} \frac{A-B}{2}$	
$\operatorname{sen} A - \operatorname{sen} B = 2 \cdot \operatorname{cos} \frac{A+B}{2} \cdot \operatorname{sen} \frac{A-B}{2}$	$\operatorname{cos} A - \operatorname{cos} B = -2 \cdot \operatorname{sen} \frac{A+B}{2} \cdot \operatorname{sen} \frac{A-B}{2}$	
Teorema de los senos:	$\frac{a}{\operatorname{sen} A} = \frac{b}{\operatorname{sen} B} = \frac{c}{\operatorname{sen} C} = 2R$	(R=radio de la circunferencia circunscrita al triángulo ABC)
Teorema del coseno: $a^2 = b^2 + c^2 - 2 \cdot b \cdot c \cdot \operatorname{cos} A$		
Área de un triángulo ABC:	$S = \frac{1}{2} b \cdot h_b = \frac{1}{2} b \cdot a \cdot \operatorname{sen} C$	$S = \frac{a \cdot b \cdot c}{4 \cdot R}$
Fórmula de Herón: (p es el semiperímetro del triángulo)	$S = \sqrt{p(p-a)(p-b)(p-c)}$	donde $p = \frac{a+b+c}{2}$

FÓRMULAS DE LOGARITMOS

$\log_a N = b \Leftrightarrow a^b = N \quad a > 0$	$\log_a M \cdot N = \log_a M + \log_a N$
$\log_a a = 1$	$\log_a \frac{M}{N} = \log_a M - \log_a N$
$\log_a 1 = 0$	$\log_a M^N = N \cdot \log_a M$
$\log_a a^m = m$	$\log_a M = \frac{\log_b M}{\log_b a}$
Si $a = 10 \rightarrow \log_a N = \log N \rightarrow$ (logaritmos decimales) Si $a = e \rightarrow \log_a N = \ln N \rightarrow$ (logaritmos neperianos)	NOTA : $e = \lim_{n \rightarrow +\infty} \left(1 + \frac{1}{n}\right)^n = 2.718281\dots$